

CELLULAR AUTOMATION OF GALACTIC HABITABLE ZONE

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Abstract. We present a preliminary results of our Galactic Habitable Zone (GHZ) 2D probabilistic cellular automata models. The relevant time-scales (emergence of life, it's diversification and evolution influenced with the global risk function) are modeled as the probability matrix elements and are chosen in accordance with the Copernican principle to be well-represented by the data inferred from the Earth's fossil record. With Fermi's paradox as a main boundary condition the resulting histories of astrobiological landscape are discussed.

1. INTRODUCTION

Since its introduction about a decade ago (Gonzalez, Brownlee and Ward 2001; cf. the review of Gonzalez 2005), the concept of Galactic Habitable Zone (GHZ) has been gaining momentum as a flexible platform for advanced astrobiological computer simulations of the Galaxy. In a simplified version, GHZ is an annular ring in the plane of the Galactic disk with sufficient metallicity for rocky planets formation and satisfying other habitability conditions such as dynamical stability and limited number of catastrophic explosions (supernovae, gamma-ray bursts). In the most restrictive approach so far (Lineweaver 2001) the ring spans between 7 and 9 kpc, and is slowly widening while moving outwards with cosmic time, mainly because of the Galactic chemical evolution. In previous papers (e.g., Ćirković and Vukotić 2008), we have used simplified 1D numerical models in order to derive most general applicability conditions for a number of astrobiological problems, like Fermi's paradox or Carter's anthropic argument. Here, we attempt to reach more detailed picture, while relying on the same concept of GHZ to investigate the present number of Galactic sites with high astrobiological complexity (i.e., developed technological civilization). Our work in this preliminary study is based on the Probabilistic Cellular Automata (PCA) approach presented below.

In brief, the PCA (like any cellular automaton) is constructed as a lattice of cells that evolve in discrete time steps (e.g., Ilachinski 2001). Each cell is allowed same several discrete states. The state of the cell in the next time step depends on the state of the cell itself and on the state of the surrounding cells in the current time step. The evolution rules are defined with the set of *transition probabilities*, thus defining the stochastic subset of cellular automata. This is particularly convenient for modelling the systems with large number of unknown or poorly understood parameters such as

GHZ. These parameters can be easily implemented and changed via the transition probabilities. Here, we will perform the PCA simulations of GHZ with variable transition probabilities. The results and input parameters will be considered in the frame of the Fermi's paradox as a boundary condition.

Fermi's paradox – the lack of traces or manifestations of extraterrestrial civilizations despite the vast amount of time since the formation of Galactic disk (for reviews see Webb 2001, Ćirković 2009) – can be viewed as a specific boundary condition for the purpose of astrobiological modelling. Here we consider two possibilities. In hard approximation the condition assumes that there are no/few extraterrestrial societies or that such civilizations are not found of expansion (see, Ćirković 2008) – this can account for the lack of the contact so far. The soft approximation puts less weight on a Fermi's paradox as a boundary condition; Either we are living in the passive corner of the Galaxy and are constantly being missed by extraterrestrial's explorations (like an Amazon forest tribe, cf. Kinouchi 2001), or our fellow Galactic cohabitants are keeping us unaware of their presence (the zoo hypothesis). Each of the two presented possibilities can be considered as a different set of transition probabilities for the purpose of computer simulation input parameters.

At present, we have no reasons to prefer one possibility over another. The output of our simulations is given as the contour plots of the developed civilization number at the end of the simulation run in the transition probabilities phase space. In the case of smooth contour plots there will still be no special reason to favour one of the two scenarios given above. However, if it turns out that contour plots show the fast changes over the transition probability phase space it will mean that some values of transition probabilities can give a plausible solution to the 'Great Silence' problem, in the light of the adopted model.

2. MODEL DESCRIPTION

The discrete cell states are: 0 - no life, 1 - simple life, 2 - complex life, 3 - technological civilization. The automation is performed on a rectangular grid with GHZ between 21st and 36th cell from the center of the grid, for the inner and outer radius of the annulus. One simulation step represents 5 Myr on the 0 - 10 Gyr time scale. The GHZ grid cells remain inactive until invoked to the state 0 according to the Earth-like planet formation rate probabilities distribution from Lineweaver (2001). In this simple model each cell is a representative of one stellar system with the main sequence host star life time chosen randomly for the 0.6 – 1.3 m_{\odot} mass range (the plausible range for habitable Solar-like systems). If the main sequence life time expires before the end of the simulation run the cell is made inactive until again invoked by the mentioned probability distribution before the simulation run ends.

Table 1 lists transition probabilities implemented in our model. First column gives the transition description and the last column gives the probability type. Evolution probabilities are driving the evolution of the cell residing stellar system towards higher astrobiological complexity. Catastrophic probabilities are evolution impeding and are of complexity degrading nature, while colonization probabilities define the probability for the cell to be colonized by adjacent state 3 cells.

First, the probabilities of all possible transitions are calculated as:

$$p_{ij} = \frac{A_{ij} t_i t_{\text{res}}}{t_{\text{char}(ij)}}, \quad (1)$$

Table 1: Transition probabilities implemented in our simulations.

Transition	Char. time [Gyr]	Amplitude	Type
$0 \rightarrow 1$	3	1.0	evolution
$1 \rightarrow 2$	0.6	1.0	evolution
$2 \rightarrow 3$	0.1	1.0	evolution
$3 \rightarrow 0$	variable	variable	catastrophic
$3 \rightarrow 1$	variable	variable	catastrophic
$3 \rightarrow 2$	variable	variable	catastrophic
$0 \rightarrow 3$	variable	variable	colonization
$1 \rightarrow 3$	variable	variable	colonization
$2 \rightarrow 3$	variable	variable	colonization

where A_{ij} is the amplitude in the $(0, 1)$ interval and is used to further control the $i \rightarrow j$ transition probability influence, t_i is the time that cell have spent in the state i , t_{res} is the simulation time step and $t_{\text{char}(ij)}$ is the characteristic time of the $i \rightarrow j$ transition probability. At initialization each cell is assigned a set of random numbers from the $(0, 1)$ interval with each element of the set corresponding to one transition. The set is reinitialized after each change of the cell state. If the transition probability is higher than a currently assigned corresponding random number then the transition is considered as pending. After this, all pending transition probabilities are stacked in an array. First probability is the first element of an array, while the sum of the second and first probability is the second element of the array and so on. The array is then normalized so the final element is one. Another random number is generated and compared with the elements of the normalized array. The transition that corresponds to the highest element of the normalized array that is smaller than generated random number, occurs.

3. RESULTS

We have performed simulation runs for various amplitudes of Table 1 probabilities and characteristic times (ranging from $10^7 - 10^8$ yr with 10^7 yr time-step, $10^8 - 10^9$ yr with 10^8 yr time-step and $10^9 - 10^{10}$ yr with 10^9 yr time-step). For the sake of brevity we present one of the smooth contour plots and one with the irregular contours (Fig. 1). For the left hand side panel in Fig. 1 transitions $3 \rightarrow 0$ and $3 \rightarrow 1$ were attenuated with $A_{30} = 0.01$ and $A_{31} = 0.1$, respectively, while the remaining transitions have amplitudes of 1.0, as is the case with the right hand side panel of Fig. 1. Also, for the right hand side panel part of the Fig. 1, $3 \rightarrow 1$ and $3 \rightarrow 2$ transitions characteristic times were kept fixed at $t_{\text{char}(31)} = 600$ Myr and $t_{\text{char}(32)} = 100$ Myr, respectively. The characteristic times of the remaining transitions were varied from 10^9 to 10^{10} yr with the resolution of 10^9 yr, for both panels. The values of $t_{\text{char}(ij)}$ for colonization transitions are given on horizontal axis while catastrophic transitions values are on the vertical axis.

The irregular shape of the contours in the right hand side panel implies that the method presented in this work can give plausible solutions to the 'Great Silence' problem. Also, it demonstrates the possible island-like nature of the "archipelago of habitability" in the transition probabilities phase space. Given the largely arbitrary character of the input parameters presented here, and various model simplifications,

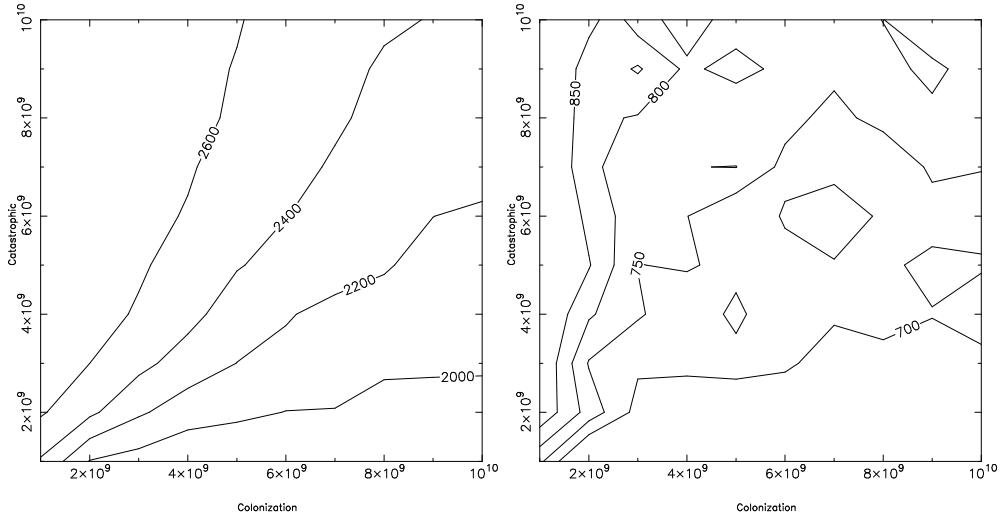


Figure 1: The contour plots of the number of cells in state 3 at the end of the simulation run for various values of input transition probabilities characteristic times. The details are given in the text.

no conclusions should be made until the results of more comprehensive future studies; obviously, more detailed results are contingent on improving results from plethora of different disciplines, notably paleobiology, (extrasolar) planetary sciences and computational physics. Instead, this work should be viewed as a form of justification for their undertaking and an illustration what modern numerical methods, unfortunately largely neglected in this field of study so far, could achieve.

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